


# High Dimensional Networks and ORA

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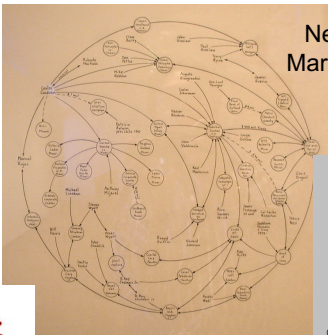
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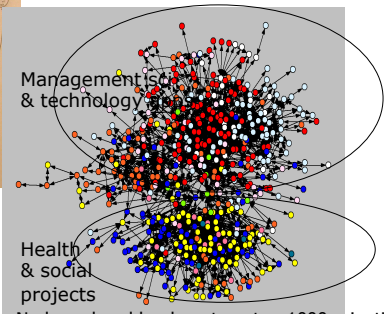
## Networks!



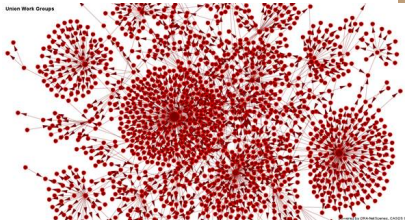
Fotosearch 2009



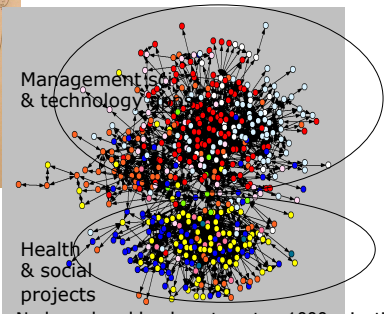
Network Art  
Marc Lombardi




Management, science & technology




Benghazi Twitter Network 2012 – Kathleen M. Carley et al.



Health & social projects  
Nodes colored by department — 1000 scientists  
Thanks to Steve Borgatti 2004



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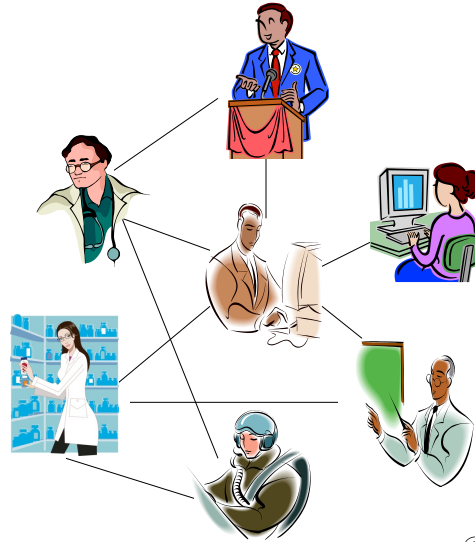
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## Social Networks

A **social network** is a description of the social structure at a particular point in time in terms of the actors (e.g., individuals or organizations) and the links among them

A **social network** indicates the ways in which the actors are connected through various social familiarities ranging from casual acquaintance to close familiar bonds.



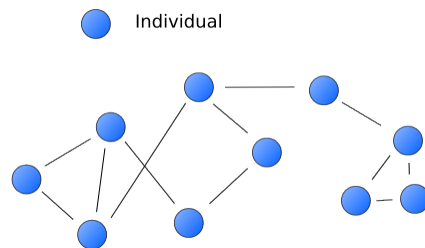
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## Traditional Social Network Analysis

- Social network analysis [SNA] is the detection, tracking and analysis of links (social relations and flows) between people, groups, organizations, computers or other information/knowledge processing entities.
- The nodes in the network are the people and groups while the ties show how the nodes are linked.



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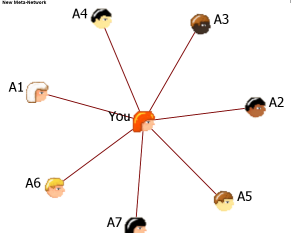
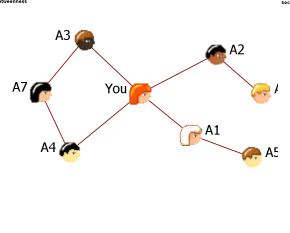
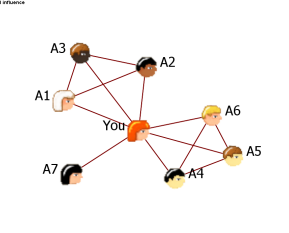
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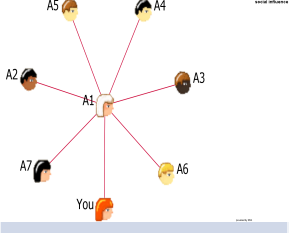
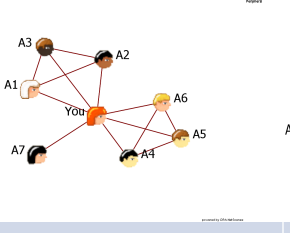
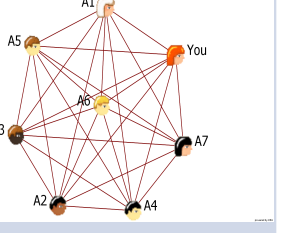


# Network Effects

Access	Control of Flows	Influence
 <p>The more people you are connected to the more you can know</p>	 <p>The more you are on the path between people the more you can control</p>	 <p>The more you are connected to others who are connected to each other the more influence they have on you and you on them</p>

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# Influence on You Network Effects

Super Spreader	Constraint	Echo Chamber
 <p>You are more likely to get information/resources from a super-spreader</p>	 <p>The more you are between multiple groups the more constrained your actions</p>	 <p>The more you are connected to others who are connected to each other the more influence they have on you</p>

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## Two Ways to Think About Networks

### What it means for the individual

- Your position in the network impacts:
  - Promotions
  - Access to information and resources
  - Health
  - Beliefs and voting behavior
  - Etc.

### What it means for the organization

- The network topology of the group impacts:
  - Efficiency
  - Resiliency
  - Speed with which information diffuses
  - Performance caps
  - Points of vulnerability

## Ego Network



- Ego – the node you are examining
- Alters – the nodes directly connected to ego
- The set of ties directly to/from ego to/from an alter
- + (sometimes) the set of ties among ego's alters

# Networks are Ubiquitous

*Nodes*

- People
- Topics
- Units of action
- Countries
- Hashtags
- Departments
- Resources
- Ideas or Skills
- Events

*Ties Between Nodes (links)*

- Transfer of resources
- Authority lines
- Association or affiliation
- Alliance
- Substitution
- Proximity
- What do you do
- Who do you like

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# Networks form Meta-Network

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## High Dimensional Networks

- Critical for Understanding and Predicting
- Have led to new insights
- Require new methods
  - From ego networks to sphere of influence
  - From centrality to weighted multi-mode centrality
  - From density to complexity
  - New metrics for
    - Overlap/Uniqueness
    - Performance
    - Cognitive demand
    - Workload
  - New Ensemble and MVMC methods for clustering
- Initial versions of all new methods are in ORA-PRO and many in ORA-LITE

## Sphere of Influence

- All ties to/from ego and the connections among the associated nodes in any meta-network
- Extension of ego net idea to meta-network
- Level = the selection path length allowed between an ego and alters in defining the size of the sphere
  - E.g., level 1 – all nodes one away from ego and the connections among them - typical ego net
  - E.g., level 2 – all nodes two away from ego and the connections among them





## Size

### Social Network

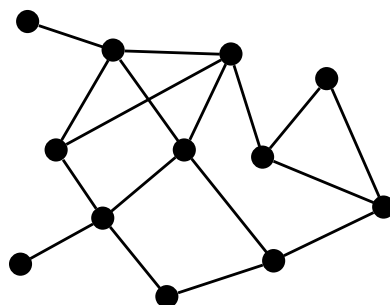
- Number of nodes (people) in the network
- As size increases
  - Density decreases
  - Clustering increases
- Reflects network boundary
- Should always be included as a covariate

### Meta-Network

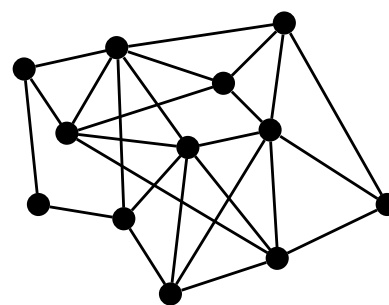
- Number of nodes of all node types
- As size increases
  - Density decreases
  - Clustering increases
  - Compartmentalization/specialization/siloing increases
  - Should always be included as a covariate
    - Or include size of each square network

## Density

- Number of ties for a single relation, expressed as percentage of the number of ordered/unordered pairs
- Number of ties / Number of possible ties
- If number of nodes =  $N$  and number of ties is  $M$ , then  $M/(N*(N-1))$  if directed and  $M/((N*(N-1))/2)$  if undirected



Low Density (25%)  
Avg. Dist. = 2.27



High Density (39%)  
Avg. Dist. = 1.76



## Complexity

- Number of ties across all relations, expressed as percentage of the number of ordered/unordered pairs for same mode and multi-mode pairs
- Number of ties / Number of possible ties
- If number of nodes across all modes = N and number of ties is M, then  $M/(N*(N-1))$  if directed and  $M/((N*(N-1))/2)$  if undirected
- Undirected may be different for square and rectangular networks

## Connect & Dis-Connect the Dots!

	Degree	Betweenness	Closeness
1	0.417 Mohamed Atta	0.334 Nawaf Alhazm	0.571 Mohamed Atta
2	0.389 Marwan Al-Shehhi	0.318 Mohamed Atta	0.537 Nawaf Alhazmi
3	0.278 Hani Hanjour	0.227 Hani Hanjour	0.507 Hani Hanjour
4	0.278 Nawaf Alhazmi	0.158 Marwan Al-Shehhi	0.500 Marwan Al-Shehhi

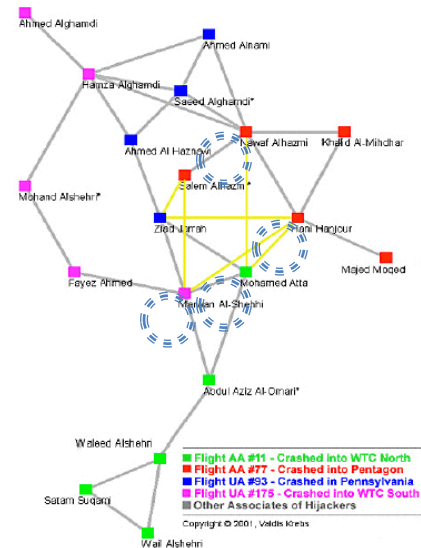


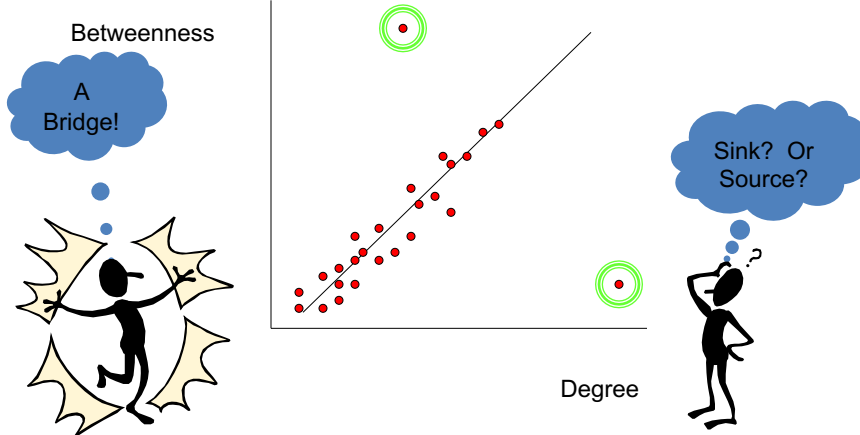
Figure 3 Trusted Prior Contacts + Meeting Ties [shortcuts]

### Standard Social Network Measures



## Moving Beyond Single Measures

**Issue: Centrality Measures are highly correlated**



## SNA Insufficient

- Centralities
  - Communication
    - Degree – most connected
    - Betweenness – most paths
- Exclusivities
  - Expertise
    - Knowledge – special expertise
    - Task – special experience
- Demands/Loads
  - Roles
    - Cognitive demand – emergent leader
    - Workload
- Performance
  - Classification

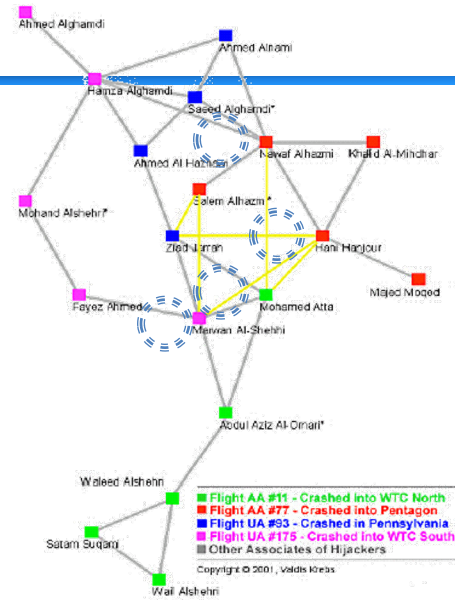


Figure 3. Trusted Prior Contacts + Meeting Ties [CASOS]

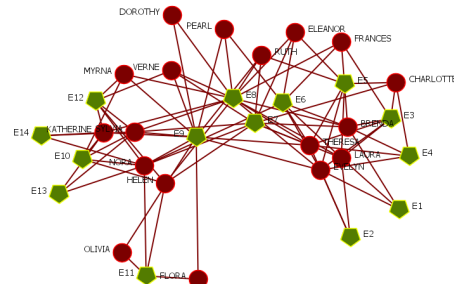
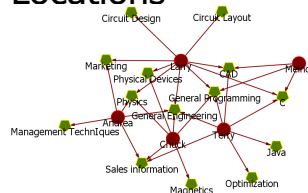


## Metrics come in Modes!

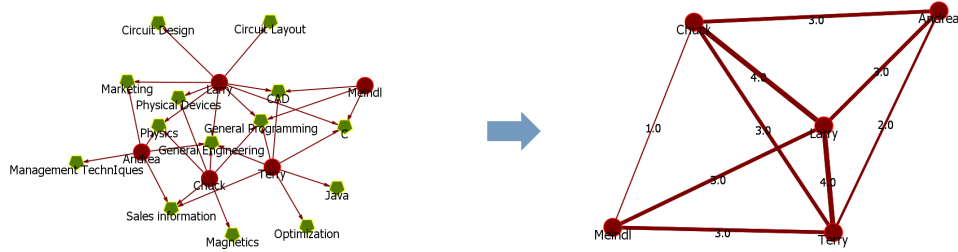
- 1 Mode Metrics
  - E.g. all centralities
  - Assumes network is square – and rows=columns e.g. social network
- 2 Mode Metrics
  - E.g. all redundancies
  - Assumes you have two types of nodes e.g. agents by events
- N Mode Metrics
  - E.g. cognitive demand
  - Assumes you have N types of nodes e.g. entire meta-network

## Two-Mode Data

- “Indirect” Connection
  - Co-Publishing, memberships in clubs, boards of companies
  - Events
- Shared ...
  - Knowledge, Resources
  - Tasks, Locations



## Approach: Folding Networks



Person	Avg. Shared Knowledge
Larry	3.50
Terry	3.00
Chuck	2.75
Andrea	2.00
Meindl	1.75

Faust (1997), Borgatti and Everett (1997)

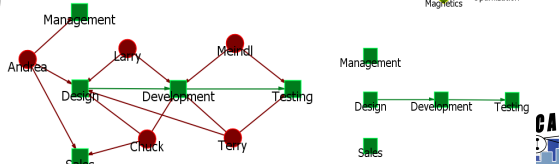


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## Approach: Meta-Networks

Meta-Matrix entities	People	Knowledge/Resources	Events/Tasks	Groups/Organizations
People	Social network	Knowledge Network/ Resource Network	Attendance Network/ Assignment Network	Membership network
Knowledge/Resources		Information Network/ Substitution Network	Needs network	Organizational capability
Events/Tasks			Temporal Ordering/ Task Flow/ Precedence	Institutional support or attack
Organizations				Interorganizational network

Krackhardt & Carley (1998)  
Carley (2002)



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## Many Specific Two-Mode Metrics

- Current ORA measures:

columnDegreeCentrality, inDegreeCentrality, outDegreeCentrality, rowDegreeCentrality, columnCount, rowCount, edgeCount, capability, knowledgeLoad, resourceLoad, density, rowBreadth, columnBreadth., columnDegreeCentralization, inDegreeCentralization, outDegreeCentralization, rowDegreeCentralization, knowledgeDiversity, resourceDiversity, relativeCognitiveSimilarity, cognitiveSimilarity, relativeSimilarity, correlationSimilarity, relativeCognitiveDistinctiveness, cognitiveDistinctiveness, correlationDistinctiveness, relativeCognitiveResemblance, cognitiveResemblance, correlationResemblance, relativeCognitiveExpertise, cognitiveExpertise, relativeExpertise, correlationExpertise, knowledgeExclusivity, resourceExclusivity, taskExclusivity, exclusivityComplete, exclusivity, columnRedundancy, rowRedundancy, knowledgeRedundancy, accessRedundancy, resourceRedundancy, assignmentRedundancy, knowledgeAccessIndex, resourceAccessIndex,

- Classification: Four concept groups of measures
- Node level + dyad level + network level metrics
- [Knowledge] for any kind of affiliation (events, ...)



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## 4. Specialization

### Identify agents that have either exclusive or redundant connections

- Exclusivity
  - Node: Exclusively connected to [knowledge]
  - *Ashworth and Carley (2006)*
- Redundancy
  - Network: different agents sharing the same knowledge.
  - Carley (2002)
- Access
  - Node: Critical connections to [knowledge]
  - *Ashworth and Carley (2006)*

$$x_i = \sum_{j=1}^{|K|} [AK(i, j) \cdot \exp(1 - \sum AK(:, j))]$$



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## Illustration of Specialization: Redundancy

- Modes: Agents x Tasks
- Average number of redundant agents assigned to tasks. An agent is redundant if there is already an agent assigned to the task.
- Redundancy occurs only when more than one agent is assigned to a task. Define the assignment redundancy for task  $j$  as follows:

$$d_j = \max\{0, \text{sum}(AT(:, j)) - 1\} \quad 1 \leq j \leq |T|$$

- Then Assignment Redundancy =

$$\left( \sum_{j=1}^{|T|} d_j \right) / |T|$$

## Illustration of Control: Cognitive Demand

*The cognitive effort the individual has to do on average*

- How many people do you interact with **CENTRALITY**
- How many tasks do you do
- How much knowledge do you have
- How much knowledge is needed to do the tasks
- How many people do you need to interact with to do the tasks
- How many other tasks and so people depend on you
- How many other tasks and so people do you depend on

## K-Shell Decomposition

- Given an undirected graph  $G=(V,E)$ , k-shell decomposition works in a series of steps iteratively:
- $k=1$ : we start by removing all nodes with degree 1 and the associated edges; assign these nodes to 1-shell
- $k=2$ : we remove all nodes of (remaining) degrees of 2 or less, and the associated edges; assign these nodes to 2-shell
- ....
- $k$ -shell: we remove all nodes of (remaining) degrees of  $k$  or less, and the associated edges; these nodes are  $k$ -shell nodes
- ...
- The process stops when no nodes are left. The last  $k$  is  $k_{max}$
- $k$ -core: the graph formed by the nodes that have not been removed at step  $k$
- $k$ -crust: the graph formed by all the nodes in  $k'$ -shells,  $k'=1, \dots, k$

## K-Shell Decomposition: k-Shell Index & Network Structures

- Besides its degree, now each node is also assigned a  $k$ -shell index
  - denote by  $shell(v)$  for a node  $v$ ; let  $deg(v)$  denotes  $v$ 's degree
  - give us another "bivariate" (or "multivariate") distribution  $\langle deg(v), shell(v) \rangle$
- Some simple facts:
  - $shell(v) \leq deg(v)$  for all  $v$ ; and clearly if  $deg(v)=1$ ,  $shell(v)=1$
  - a high degree node may have low  $k$ -shell index: for any  $v$  w/ arbitrary  $deg(v)>1$ , its  $k$ -shell index can be as low as 2
  - for  $v$ , if the largest degree of its neighbor is  $d$ , then  $shell(v) \leq d+1$
  - If  $v$  is part of  $s$ -clique (and thus  $deg(v) \geq s$ ), then  $shell(v) \geq s$ .
- Connected components in 1-crust: singleton nodes and isolated edges
- Connected components in 2-crust: stars and stars connected via a path
- .....

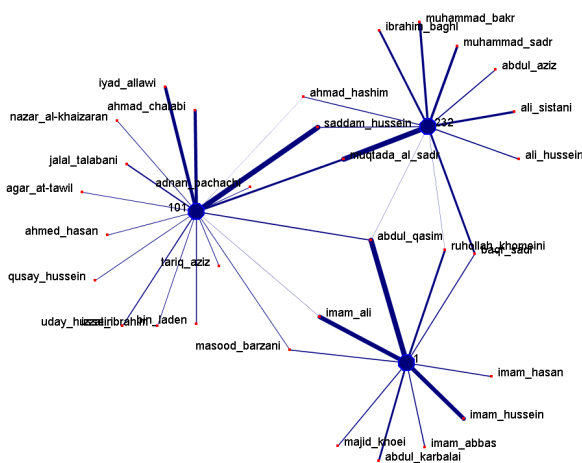


## Summary on Metrics

- Level
  - Node level
  - Dyad level
  - Graph level
- Node level
  - Direct
    - E.g. degree
  - Path based
    - E.g. betweenness
  - Iterative
    - E.g. page rank
- Graph level
  - Cohesive
    - E.g. density
  - Spread
    - E.g. characteristic path length
  - Lumpiness
    - E.g. clustering coefficient
  - Min, max, mean, std. dev of node level metrics
- 2 (and n) mode metrics
  - Folding
  - Meta-networks



## Assess: How are they organized?



**FOG (Fuzzy Group Clustering)** shows suspicious entities organized into 5 groups w/shared members.

=====  
 Interstitial members are likely to contain coordinators & leaders

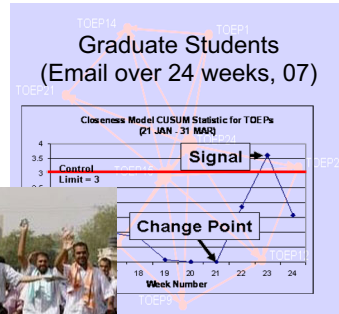
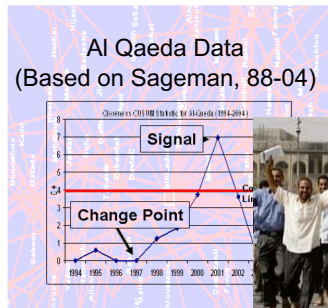




## Change Detection - Objective

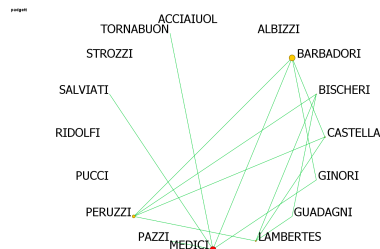
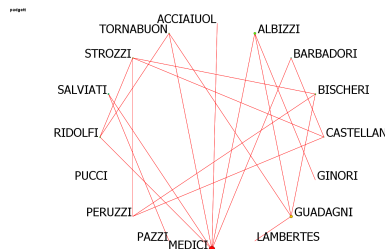


How can we quickly identify changes in social networks subject to a specified risk of false alarm?



## Compare and Contrast

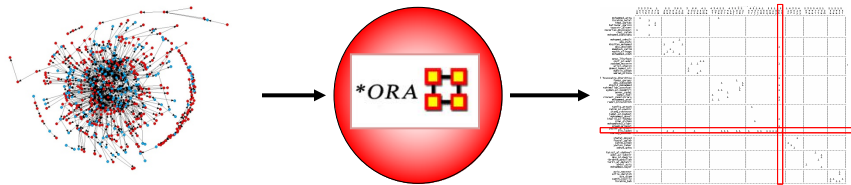
- Marriage ties
- Nodes sized by betweenness and colored by degree
- Banking ties
- Nodes sized by betweenness and colored by degree



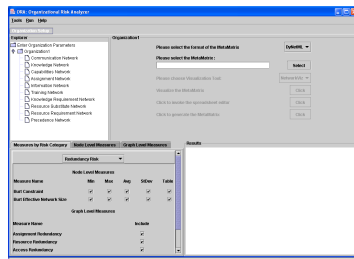
Use Tiles in ORA visualizer to Show Differences



## ORA



ORA: a DNA statistical analysis tool for locating patterns and identifying vulnerabilities



- Organized by function not measure; e.g.,
  - Key Entity Report
  - Group Locator Report
- Import/Export tools
- Linkage to mysql
- Visualization components
- Batch, web, thick-client
- Can handle large  $10^6$  networks quickly

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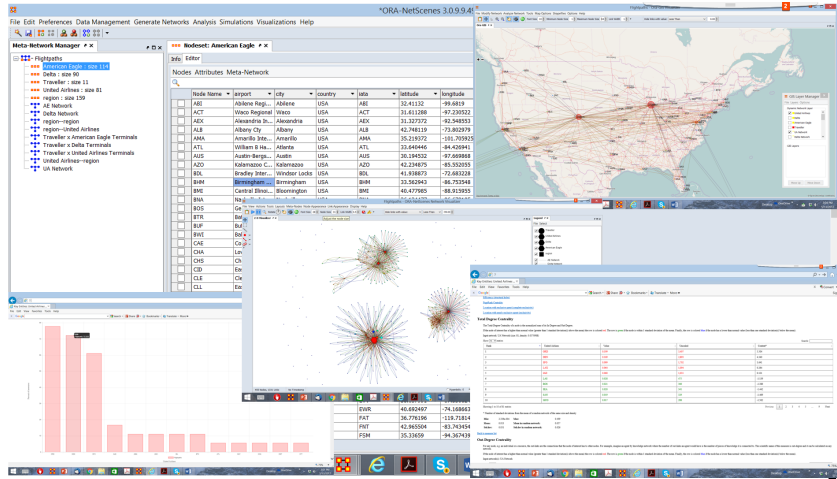
## ORA

- Network analytic and visualization toolkit
- Statistical, graph-theoretic and visual analytics for complex network data
  - Special tools for analyzing and visualizing dynamic networks
  - Special tools for geo-enabled network analysis and visualization
  - Supports 1-mode, 2-mode and meta-network calculations
- Illustrative functions for social networks or link analytic data
  - Ability to identify groups, key nodes, hidden links, critical locations
  - Ability to identify patterns of interest
  - Ability to visualize networks (2D and 3D), visualize change and network dynamics, visualize networks on maps, visualize network attributes by region (e.g., precinct level statistics)
  - Ability to analyze topics, topic groups, and identify changes in topics
- Often referred to just as ORA

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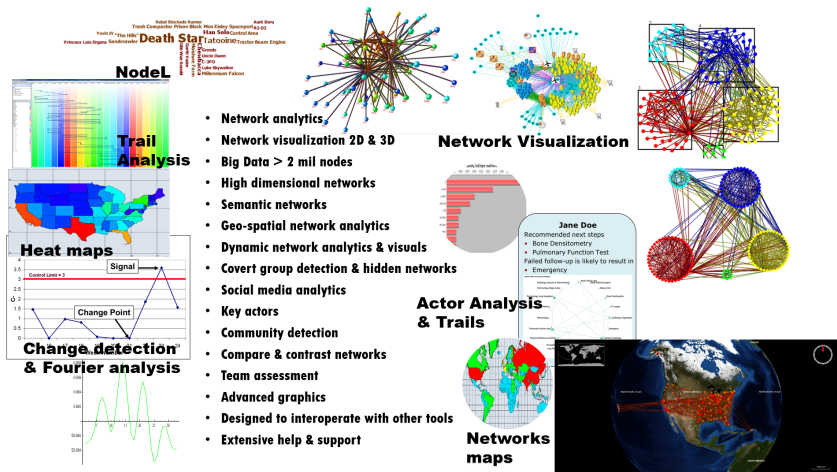


# ORA in Operation



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# ORA Visualization



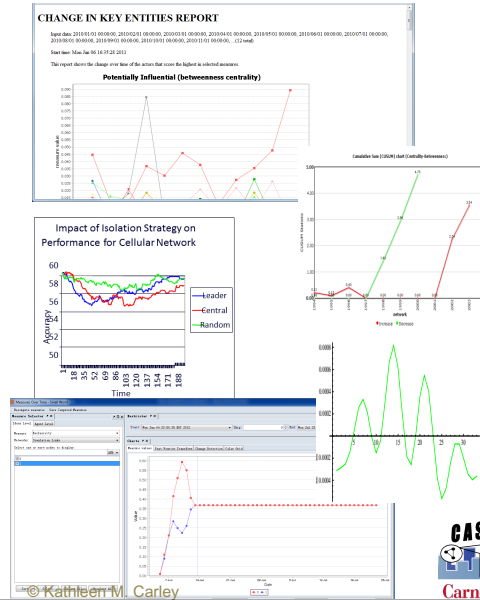
- Network analytics
- Network visualization 2D & 3D
- Big Data > 2 mil nodes
- High dimensional networks
- Semantic networks
- Geo-spatial network analytics
- Dynamic network analytics & visuals
- Covert group detection & hidden networks
- Social media analytics
- Actor Analysis & Trails
- Community detection
- Compare & contrast networks
- Team assessment
- Advanced graphics
- Designed to interoperate with other tools
- Extensive help & support

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## ORA does Dynamic Network Analysis

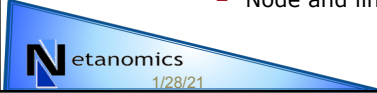
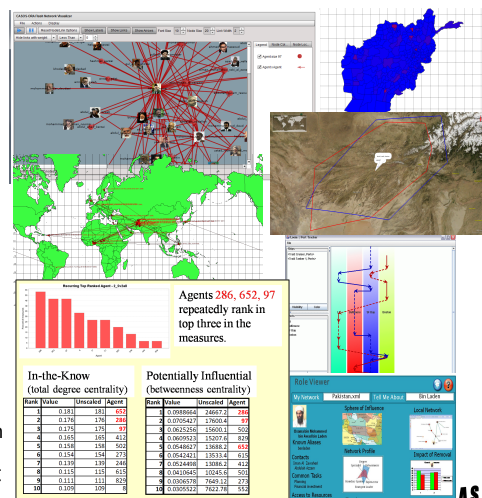
- Trends for metrics
- Trends for nodes
- Through time visualization
- Comparative statistics for two time periods
- Forensic change detection
- Fourier analysis for pattern of life assessment and anomaly detection
- Immediate impact assessment for network change
- Near term forecasting for network change



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## ORA does Geo-Enabled Dynamic Network Analysis

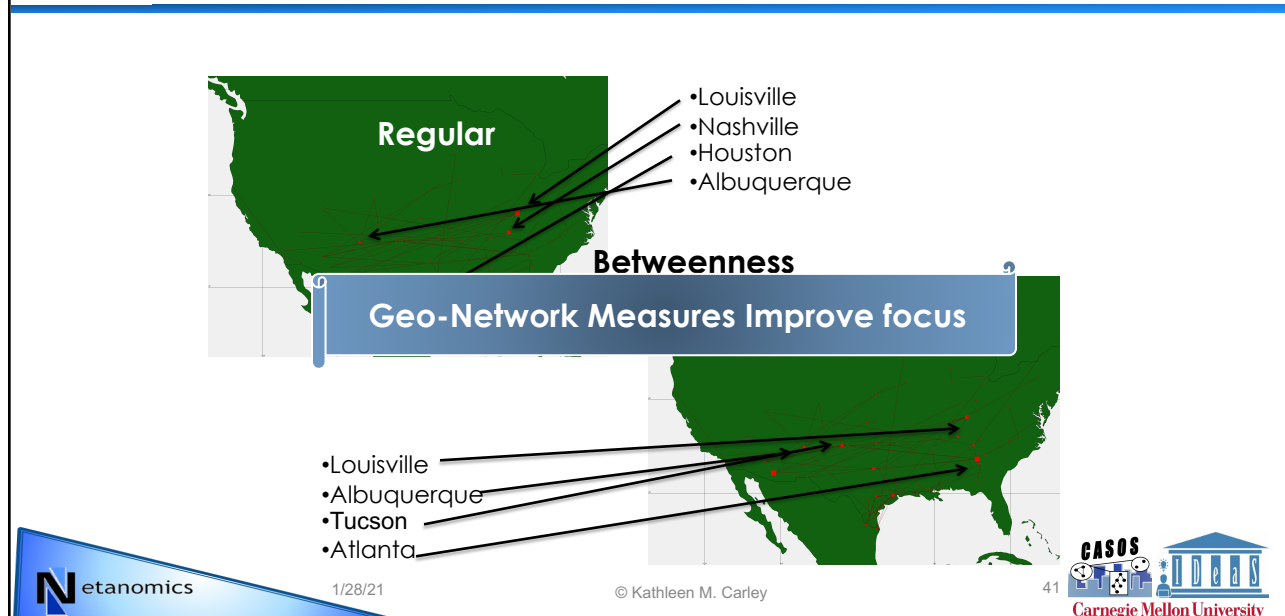
- Complex "meta" networks
  - who, what, where, how, why and when
- Key Features
  - Network visualization
  - Network analytics
    - Key actor, location, idea ...
  - Network dynamics
    - Network comparison
    - Change detection
    - Trend analysis
  - Path identification
  - Link inference
  - Trail analysis and visualization (who was where when)
  - Pattern analysis
    - Extraction of patterns of particular importance in law enforcement such as working cells
  - Node and link attribute assessment



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## Using Constraints to Set Strength of Links has Practical Consequences



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## Metrics and Grouping Capabilities

- Over 200 metrics
- Key node
  - Centralities
  - Loads
  - Redundancies
- One-mode, two-mode and meta-network metrics
- Illustrative Grouping algorithms
  - Concor
  - Newman-Girvan
  - Fog
  - Johnson-hierarchical
  - Louvaine
  - Leiden
  - Spectral
  - MDS
  - LDA
  - LSA
  - Ensemble
  - MVMC



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## Other Features

- Matrix algebra techniques
- Stylized network generation
- Supports editing for
  - Nodes
  - Edges
  - Node attributes
  - Network attributes
- Metrics organized into workflow reports
- Extensive help
- Quick-start guide
- ORA google groups



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## Interoperability & Data Control

- Data entry
  - Import wizard
  - Direct entry through visualizer
  - Ability to import from many packages
    - E.g. ucinet, i2, mysql, csv, tsv, tweettracker, blogtracker
    - Any csv, tsv, or json file can be imported
- Export visualization in multiple formats e.g. .png, gif
- ...
- Ability to generate maps for ArcGIS, google-earth, NASA Worldwind
- Data output in HTML and CSV
- Data editing, cleaning, anonimization and manipulation capabilities
- Companion tools for processing texts and twitter data



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